

Never Stand Still

Faculty of Science

School of Mathematics and Statistics

Solution Sheet 8, June 20, 2012

Answers

- 1. Use the fact that 1997^4 ends in a one. Answer is 7
- 2. 500
- 3. Pythagoras' Theorem.
- 4. Assume $x \le y$, then (7,42), (8,24), (9,18), (10,15), (12,12). Repeat for x and y swapped.
- 5. (a) 1
 - (b) The sum of the geometric series $S = 1 2 + 4 8 + \ldots + (-2)^{n-1} = \frac{1 (-2)^n}{1 (-2)} = \frac{1 + 2^n}{3}$ since n is odd. Then $3S = 1 + 2^n$, so $1 + 2^n$ is divisible by 3. Similarly $1 + 2^m$ is divisible by 3. Hence the gcd is at least 3.
- 6. ... its a rectangle.